

Binary Trees

Also Trees,
Binary Search Trees

CRACKING *the* CODING INTERVIEW

189 PROGRAMMING QUESTIONS & SOLUTIONS



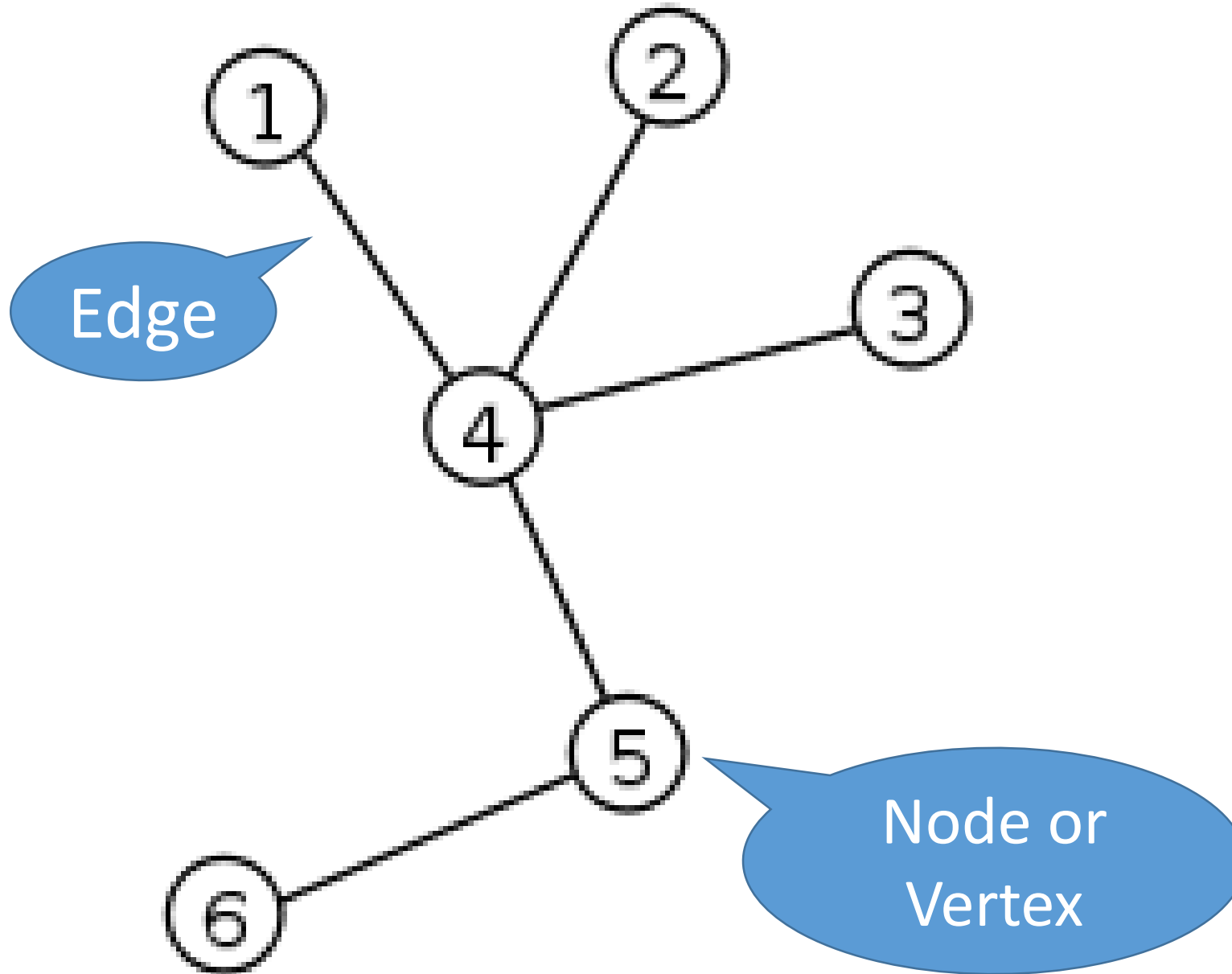
GAYLE LAAKMANN MCDOWELL **6TH** EDITION
Author of Cracking the PM Interview and Cracking the Tech Career

OXFORD

A FIRST COURSE IN NETWORK THEORY

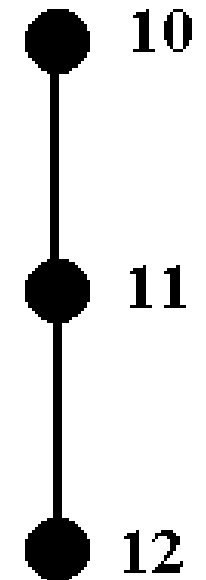
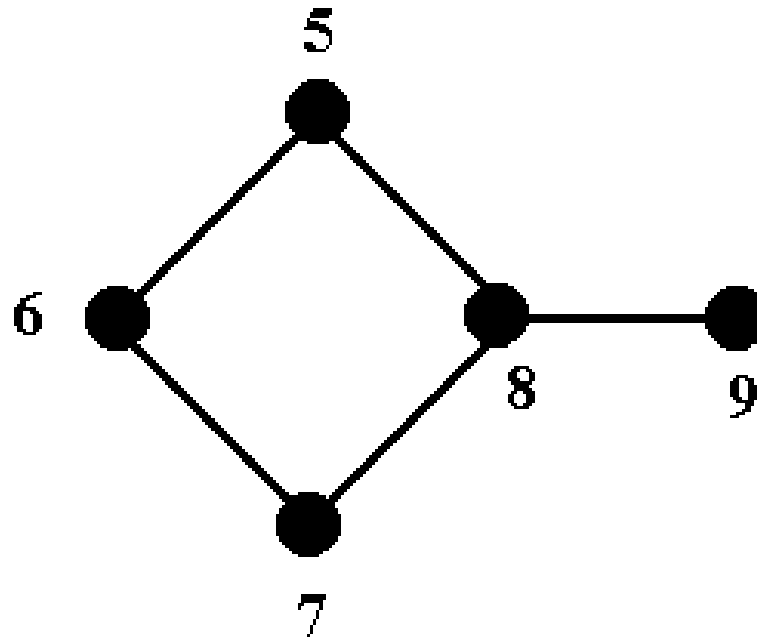
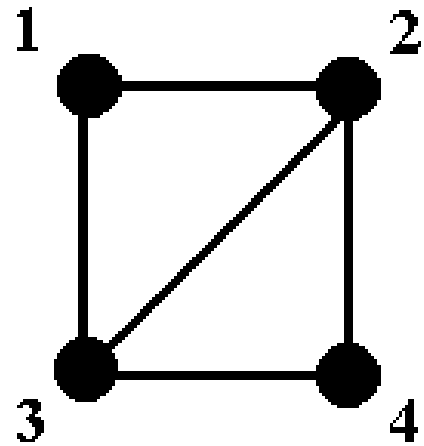
ERNESTO ESTRADA AND PHILIP A. KNIGHT





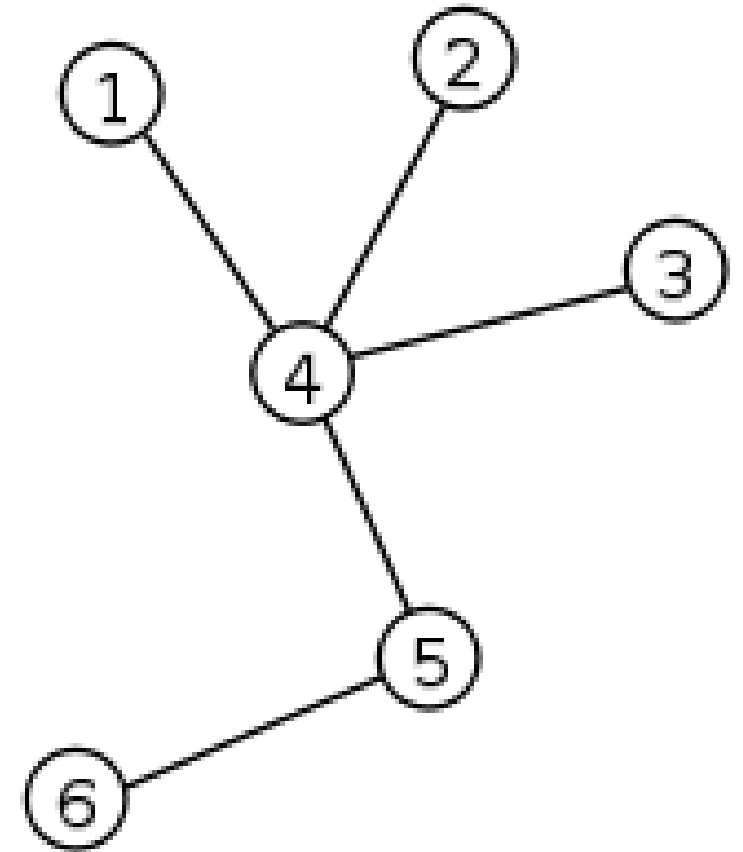
A graph is a structure constructed of nodes which are connected by edges.

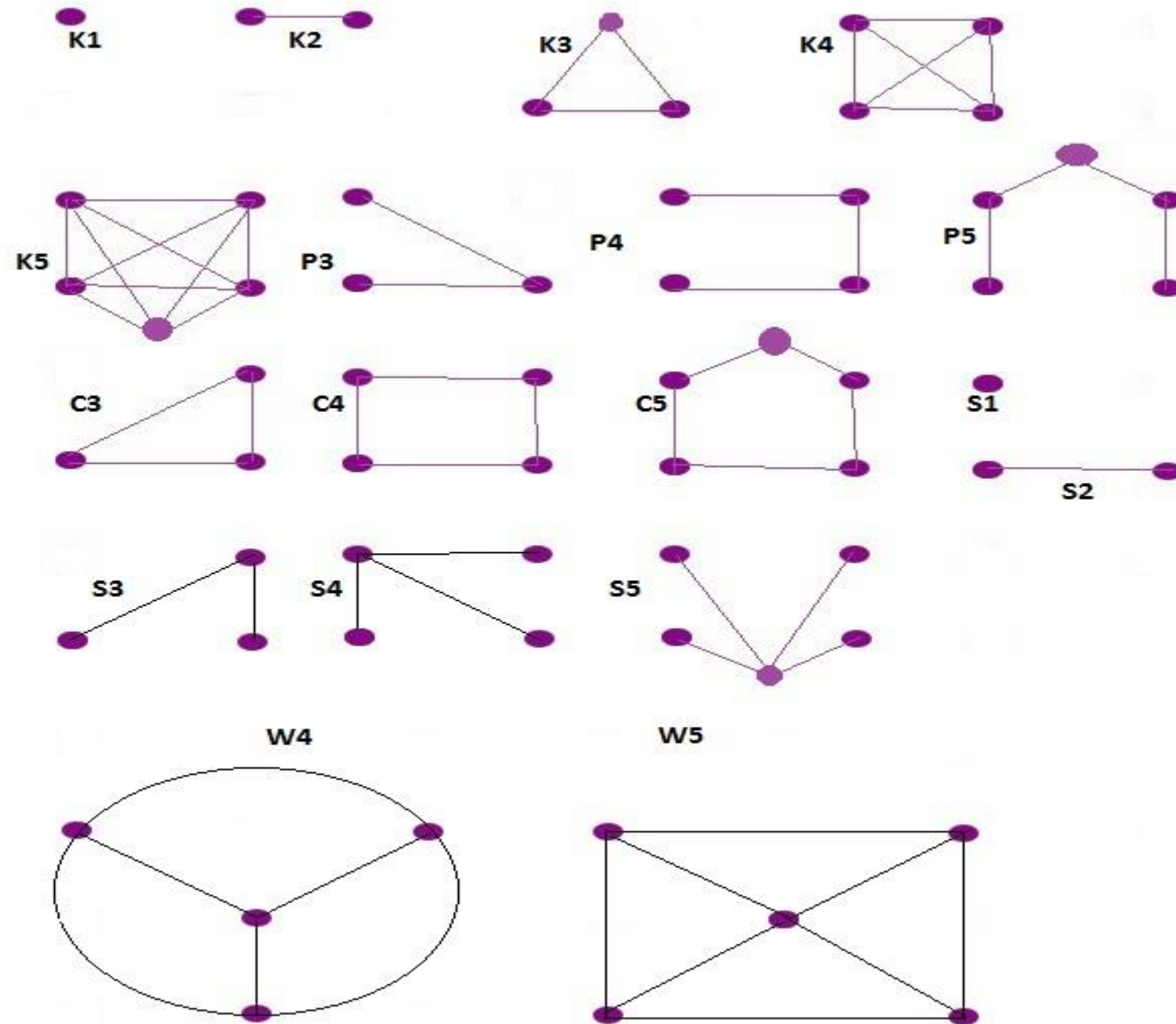
A circuit is a path through a graph that starts and ends at the same vertex.



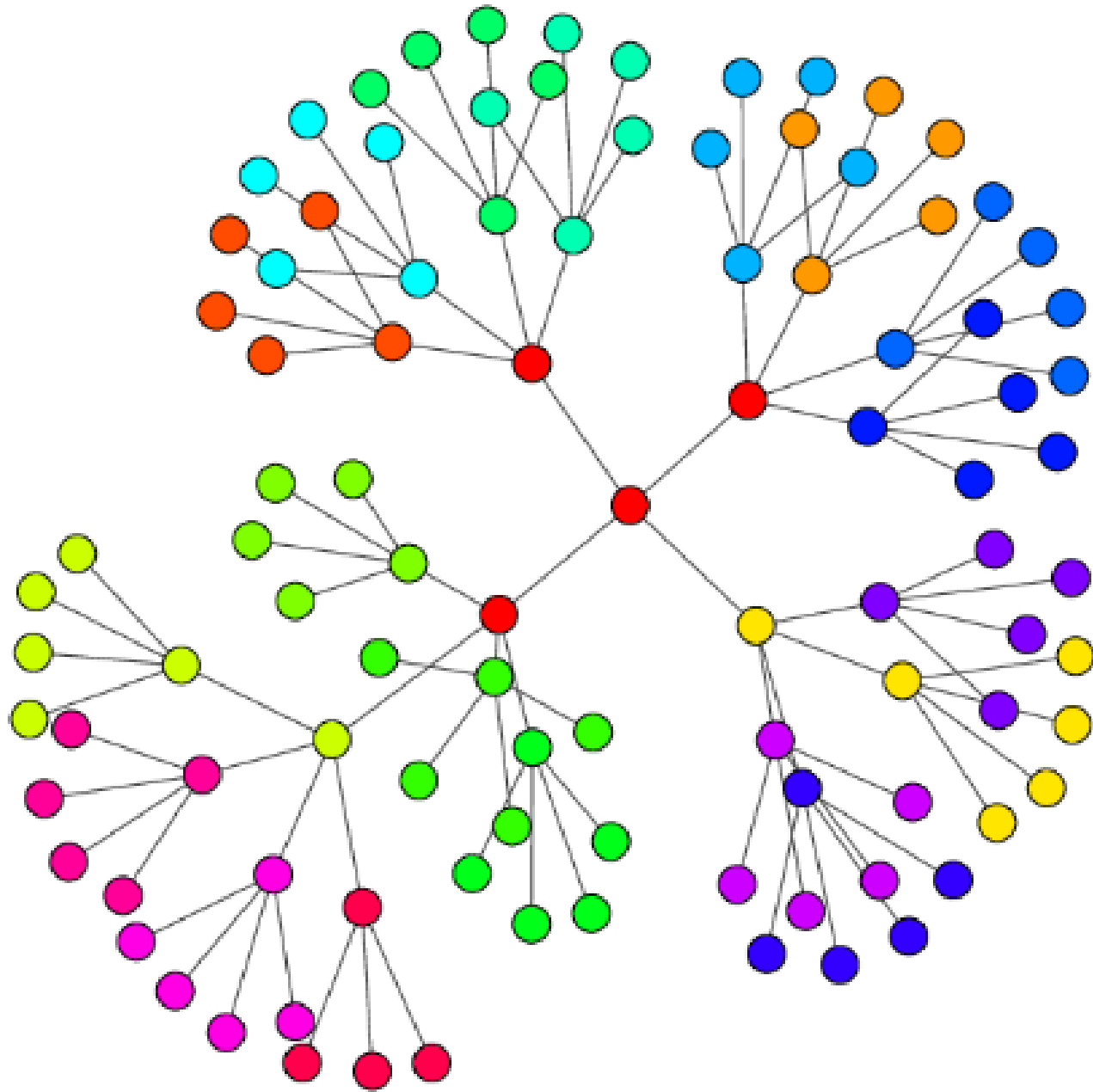
A tree is a graph in which any two vertices are connected by exactly one path.

A tree does not contain a circuit.



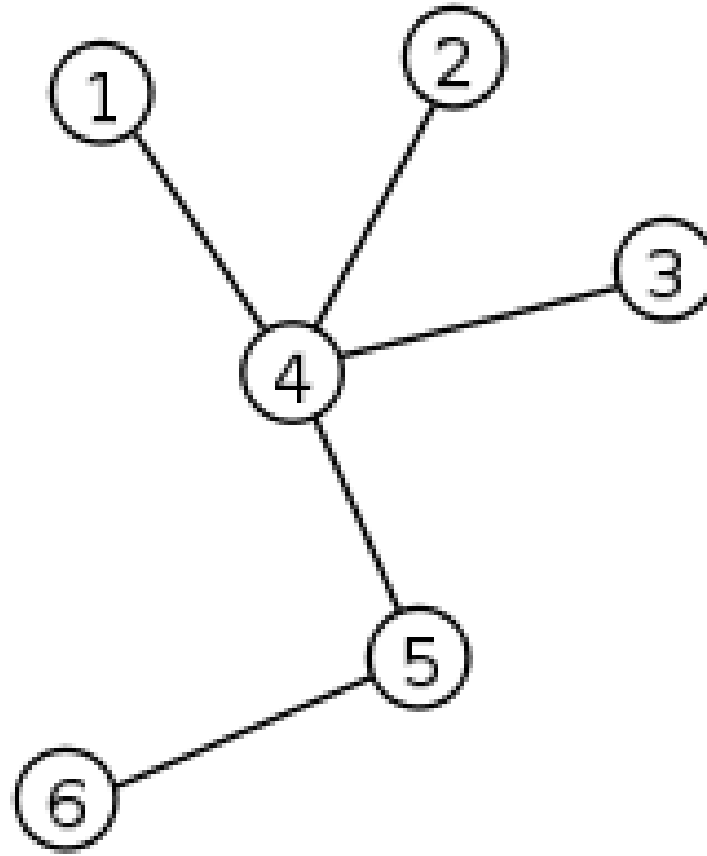


Which
are
trees?



Is this a
tree?

A tree of n vertices has $(n-1)$ edges.



Is this a tree?

THE JOB

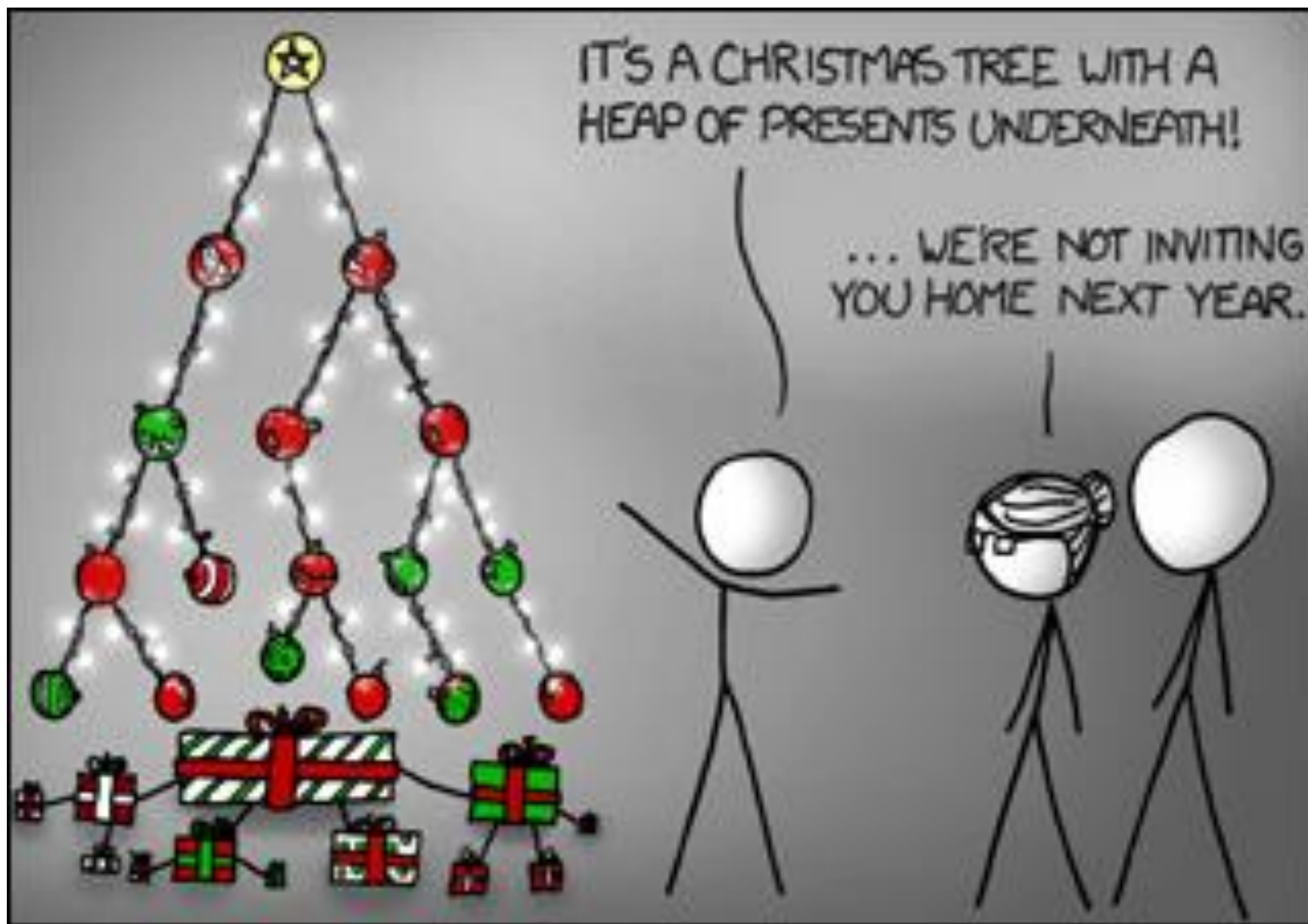
Strategic
planning
tool



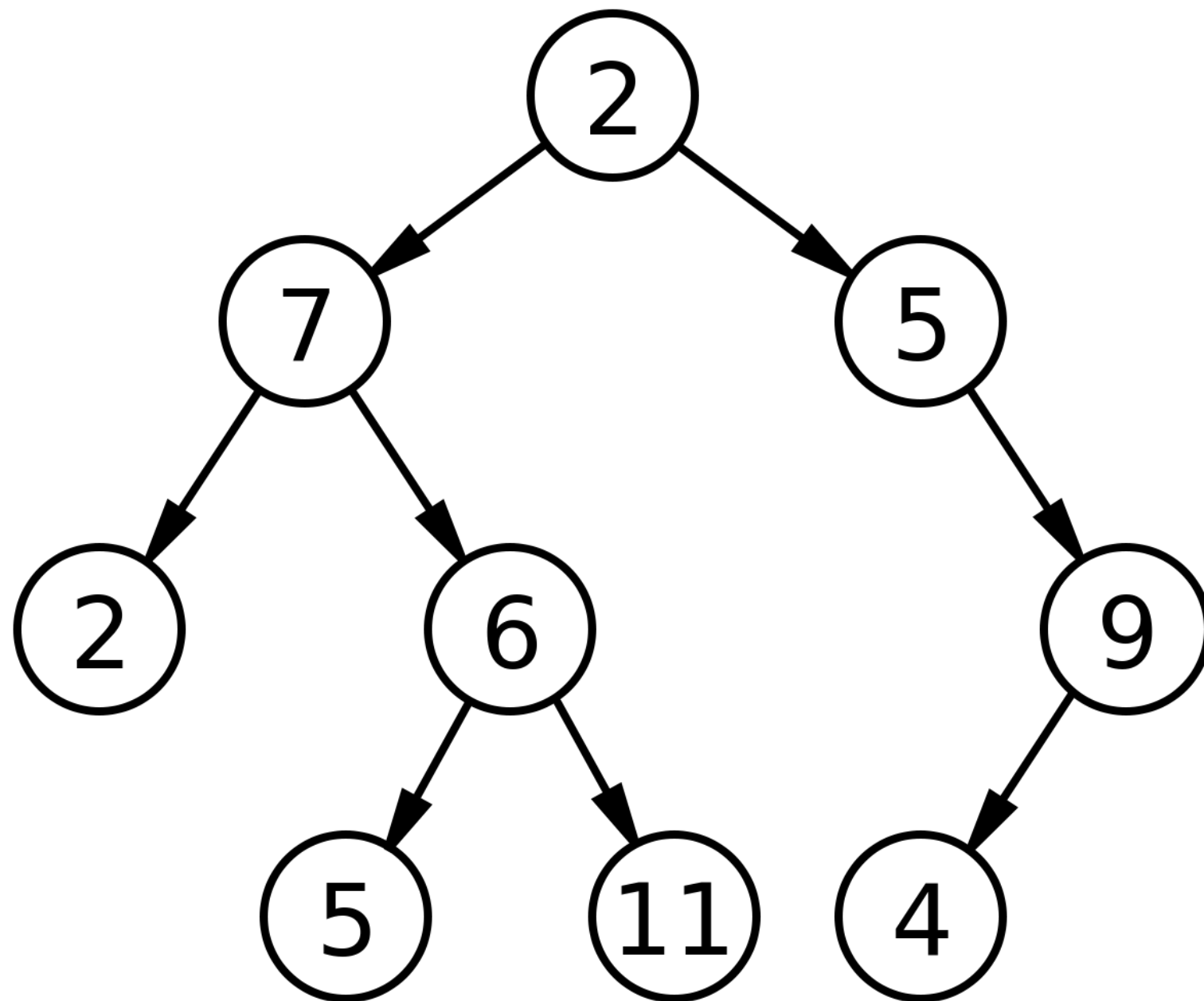
PLANT THE
DECISION TREE
THERE.

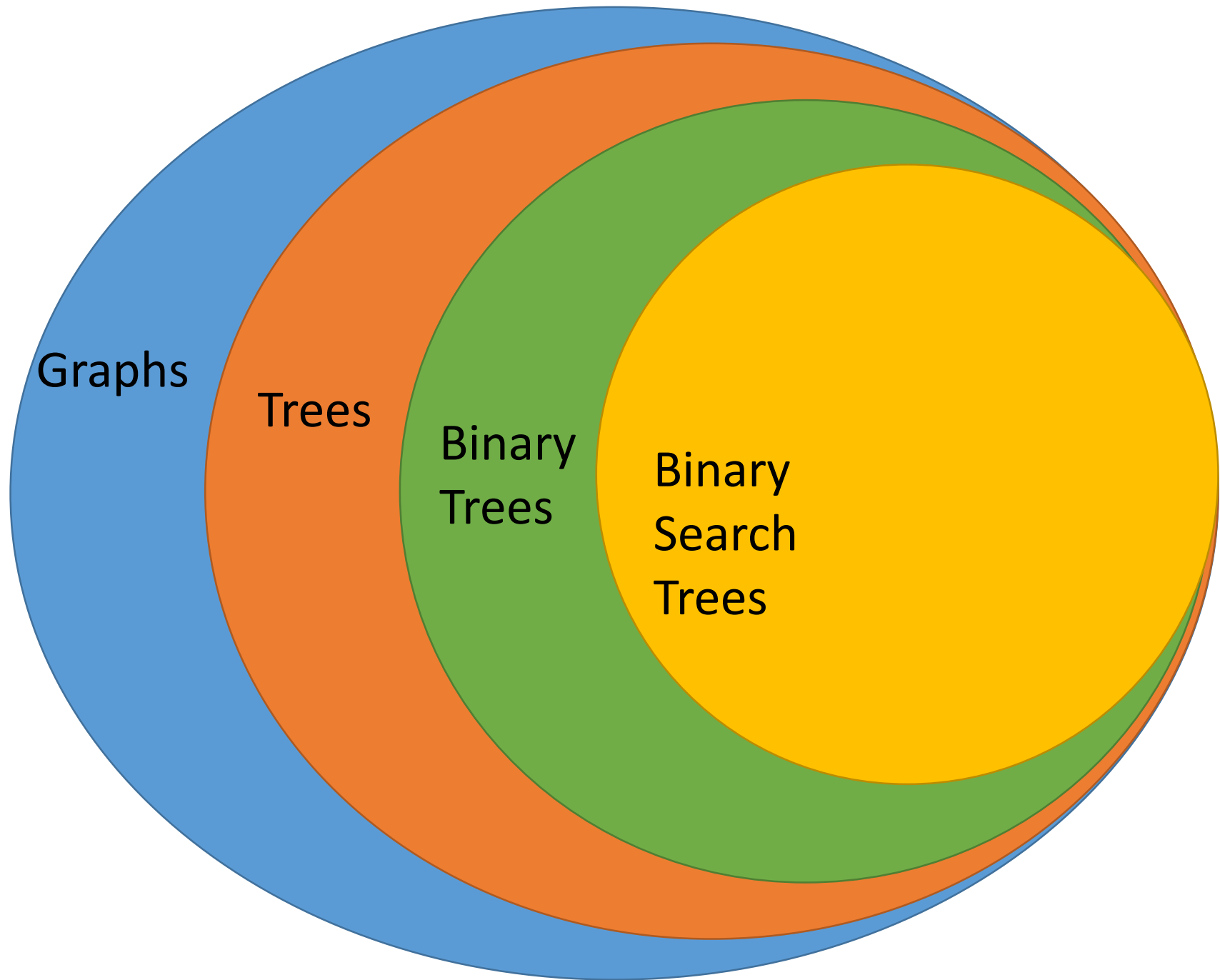


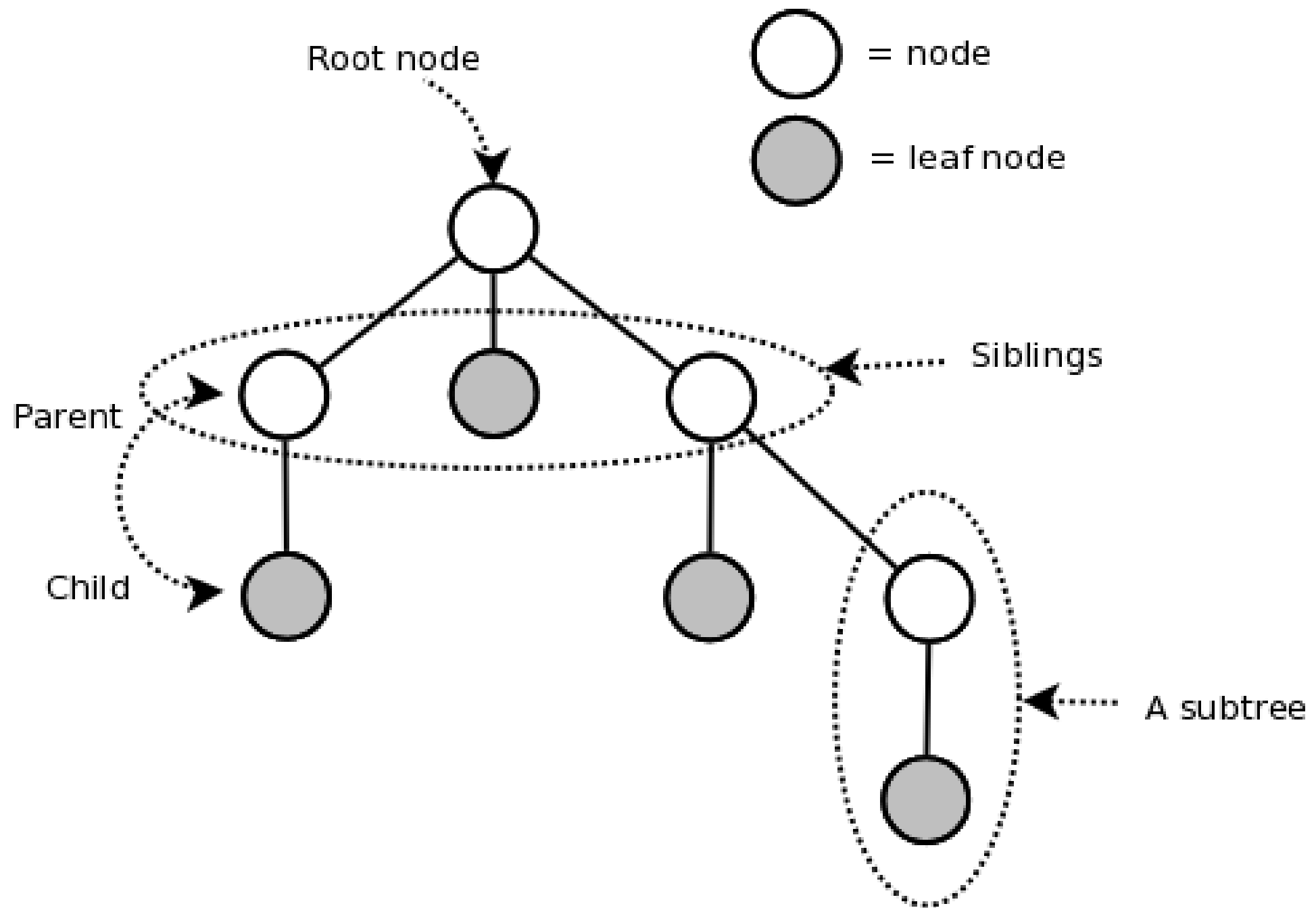
LANDSCAPING
AT THE
INDUSTRIAL
PARK.

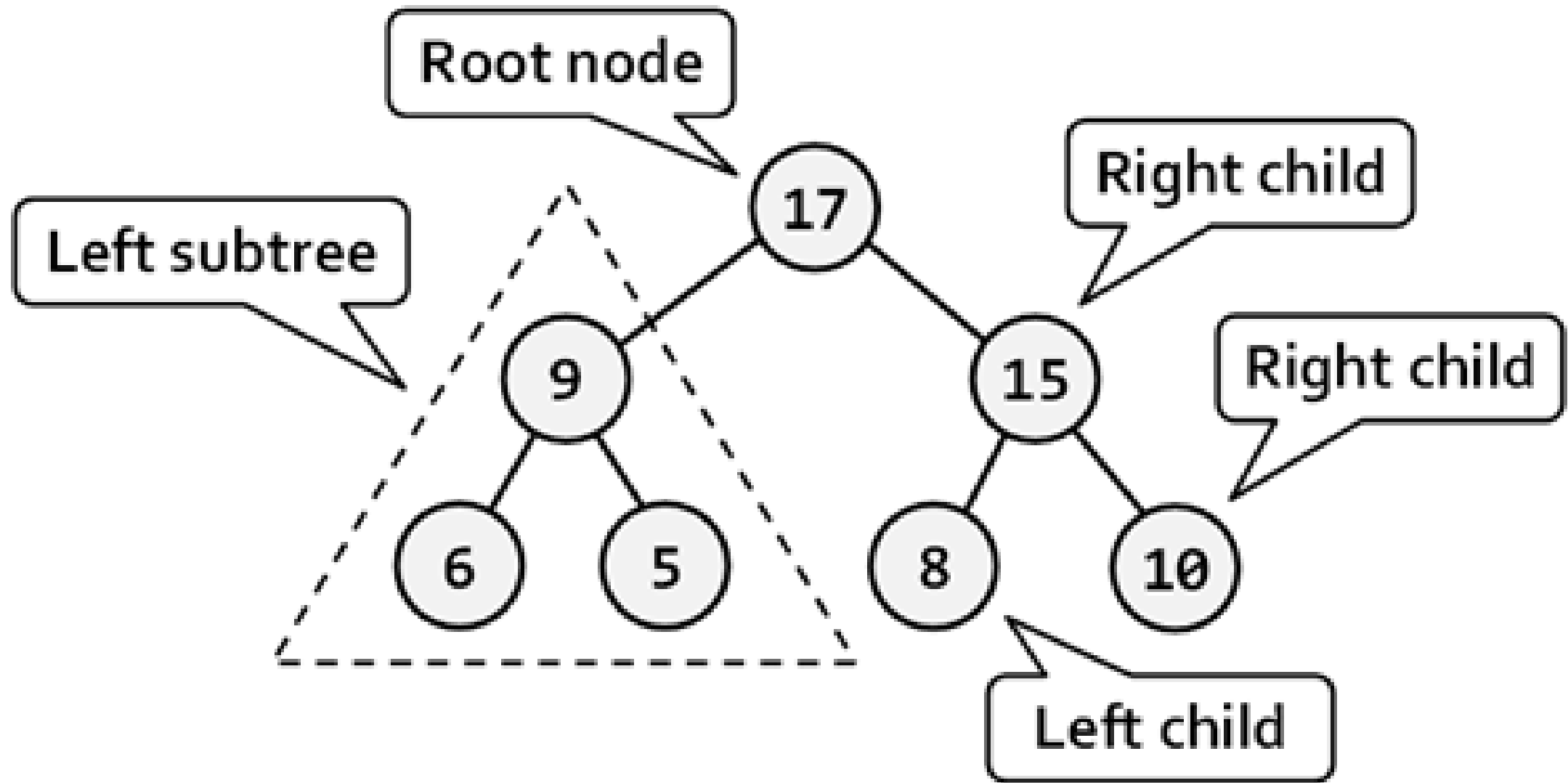


In a binary tree,
each vertex has
at most two
children.



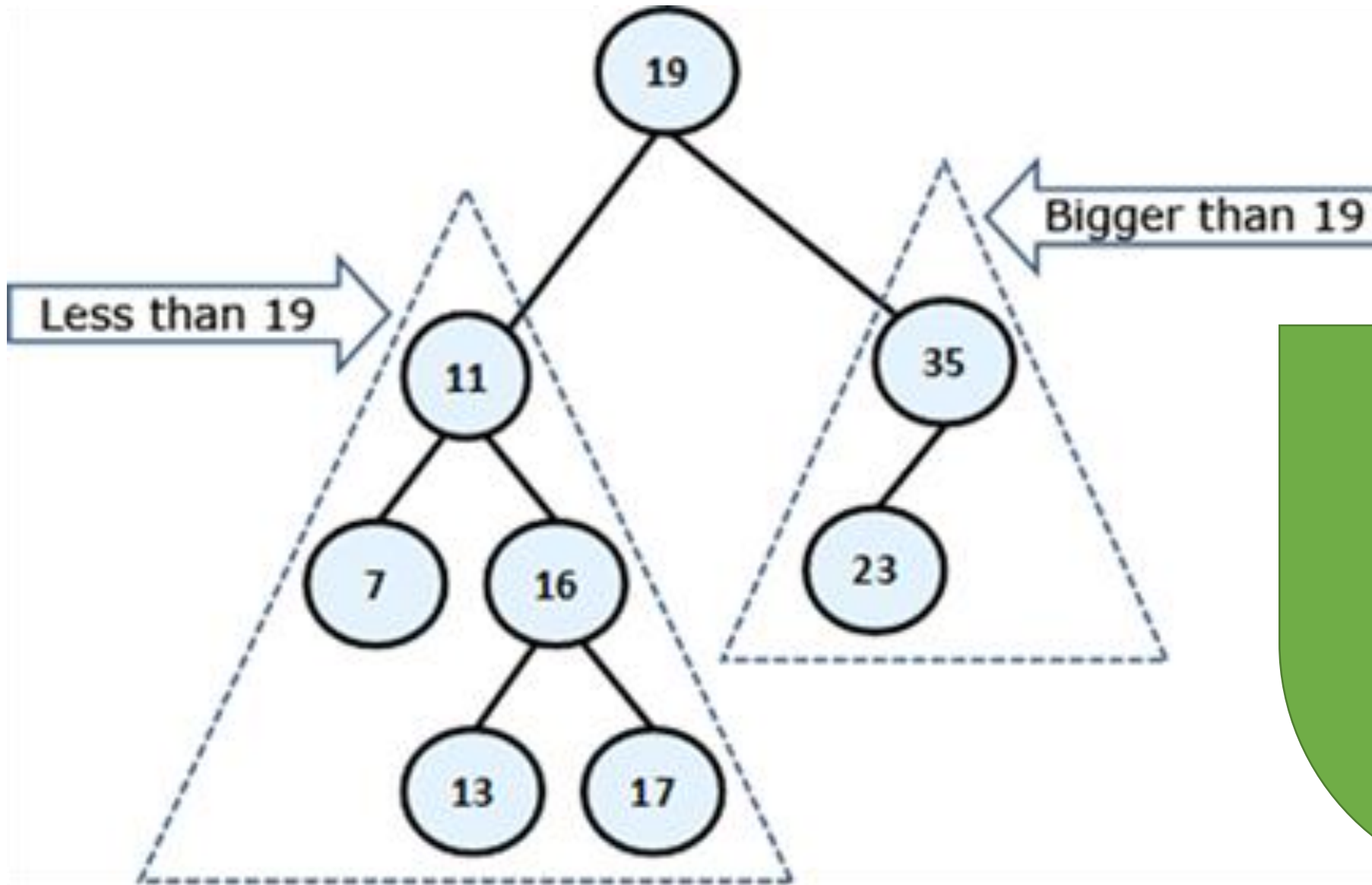




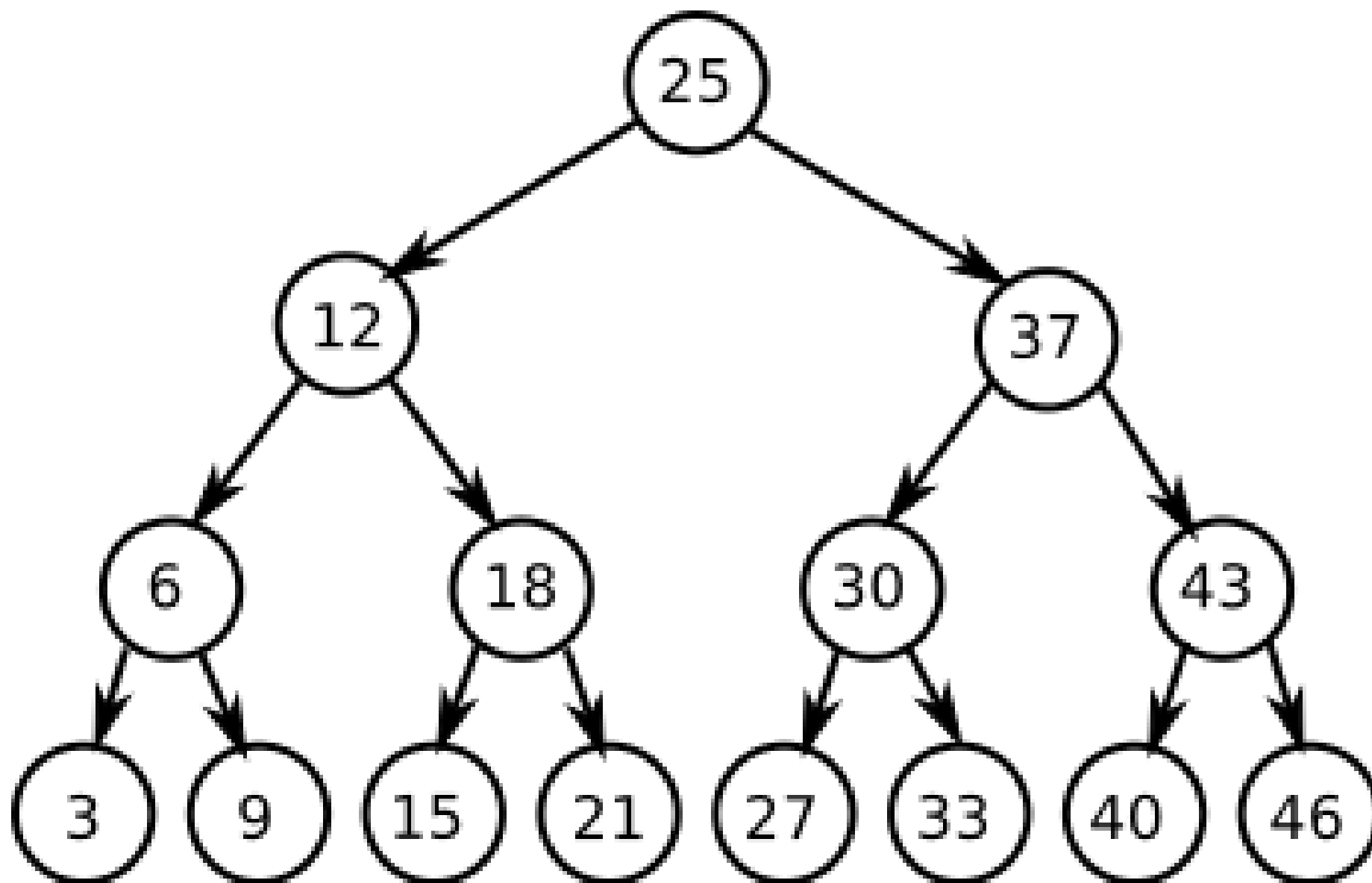


A full binary
tree with i
parent
vertices, has
 $2i+1$ vertices

Is this a
tree?



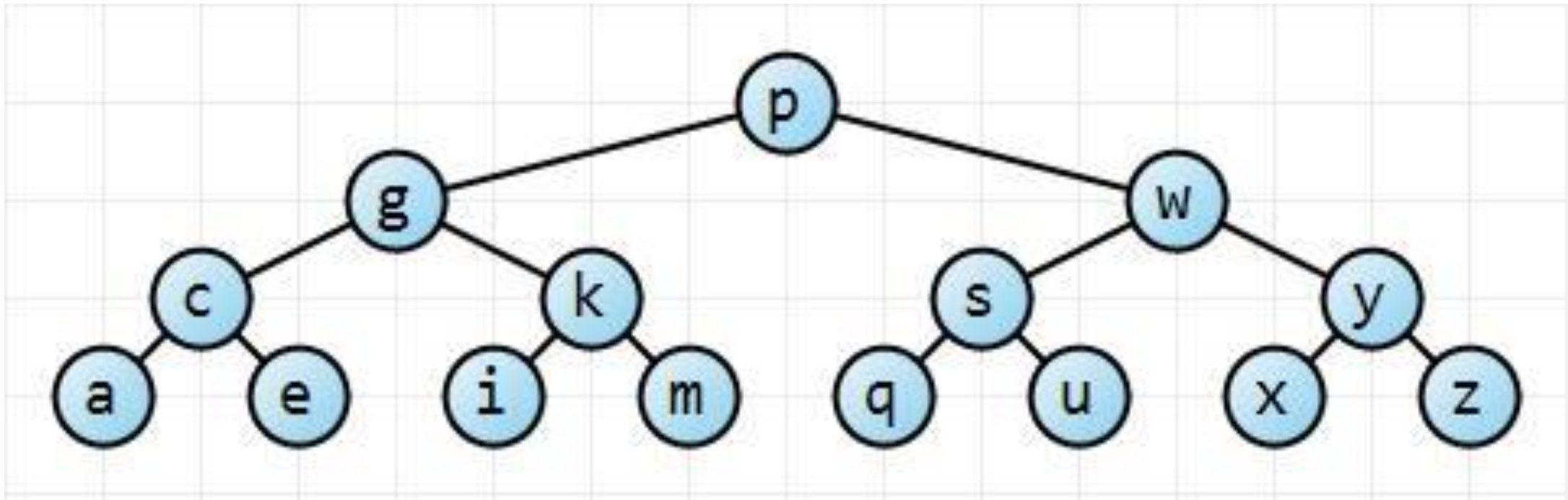
In a Binary search Tree, all of the nodes to the left of the parent are less than it, to the right, greater.



A
tree?

A
binary
tree?

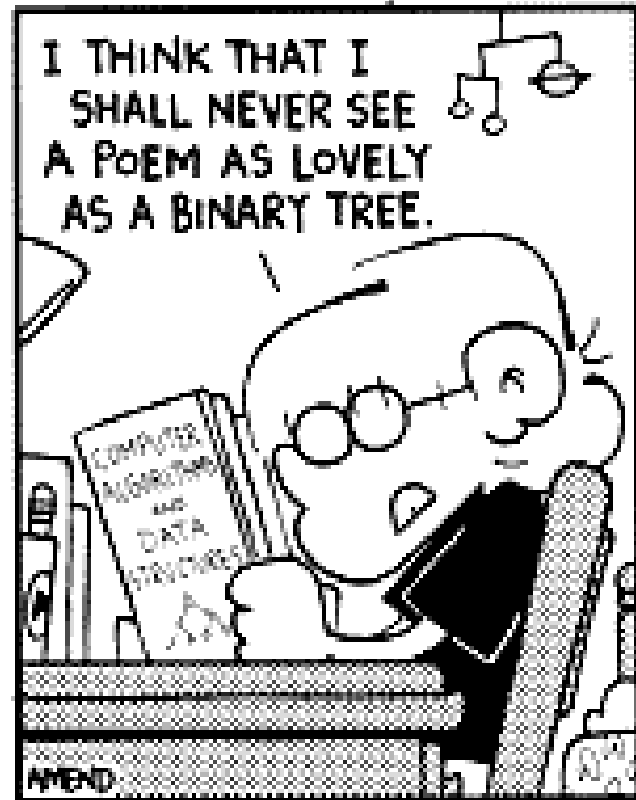
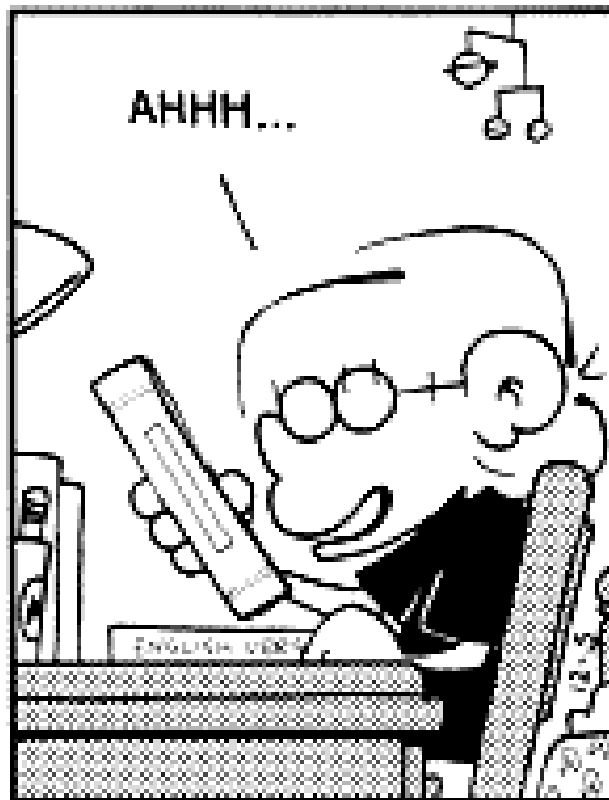
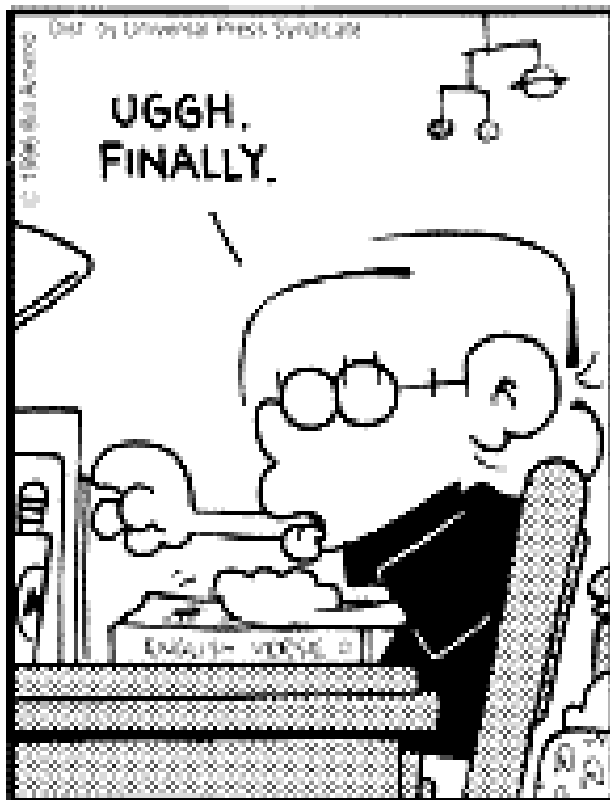
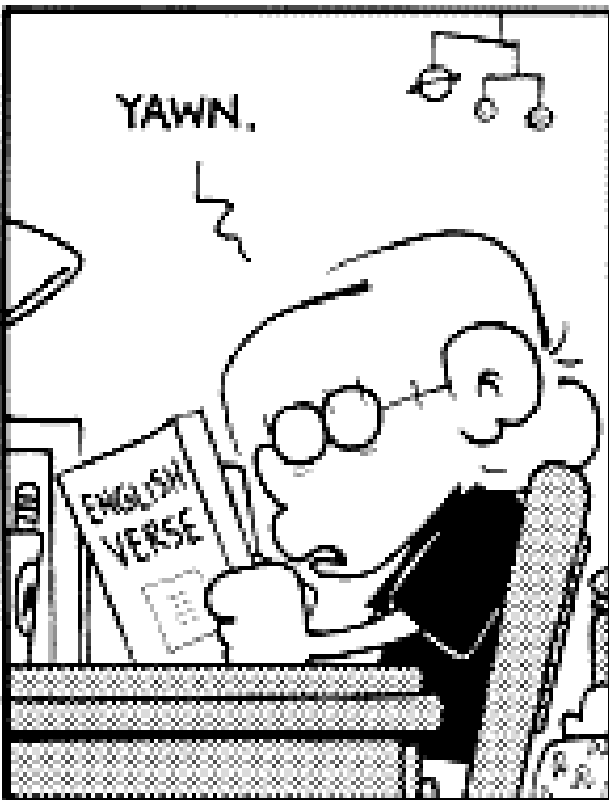
A
binary
search
tree?



A
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A
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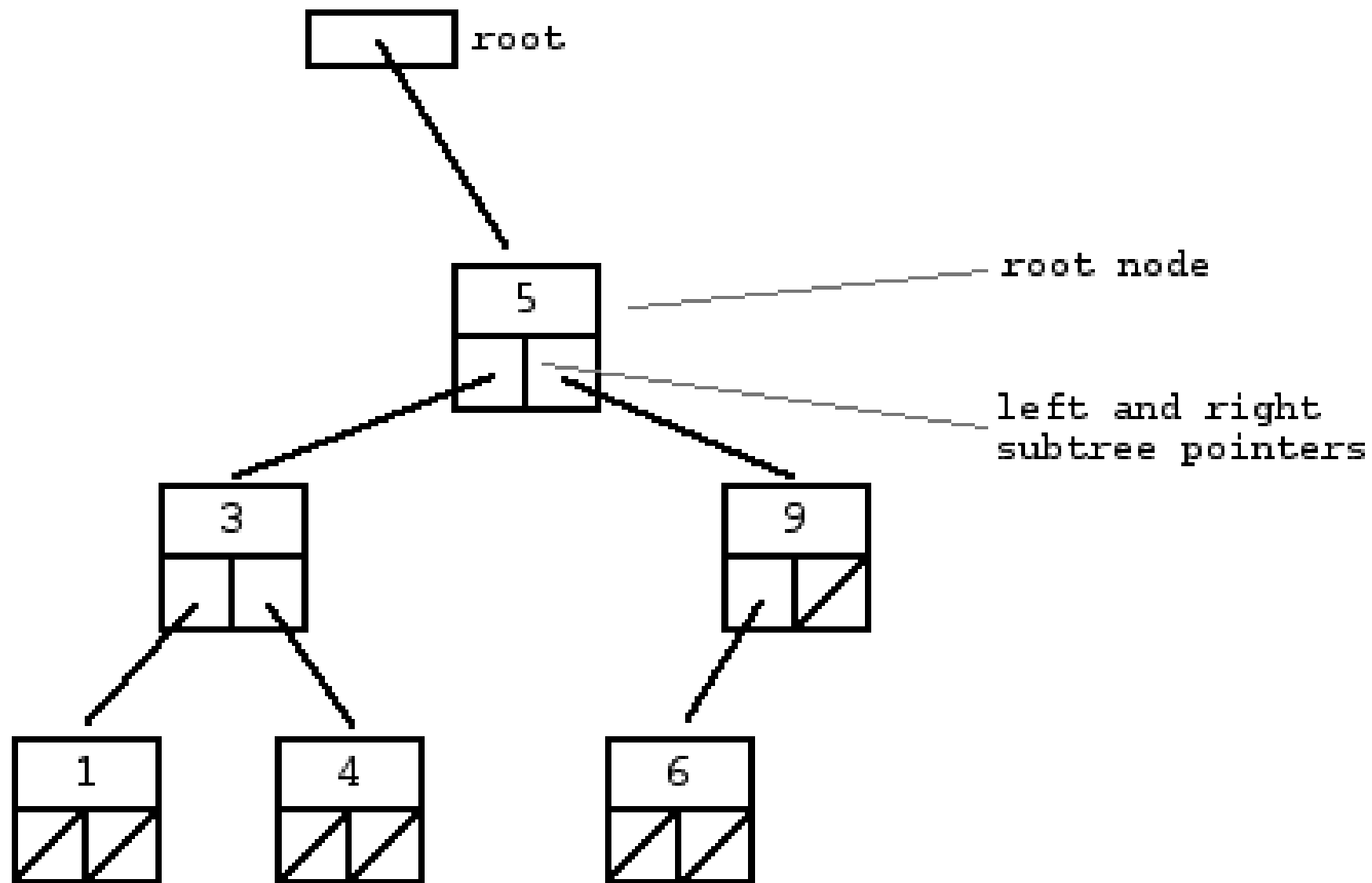
```
public class Node {  
    String key;  
    Node left, right;
```



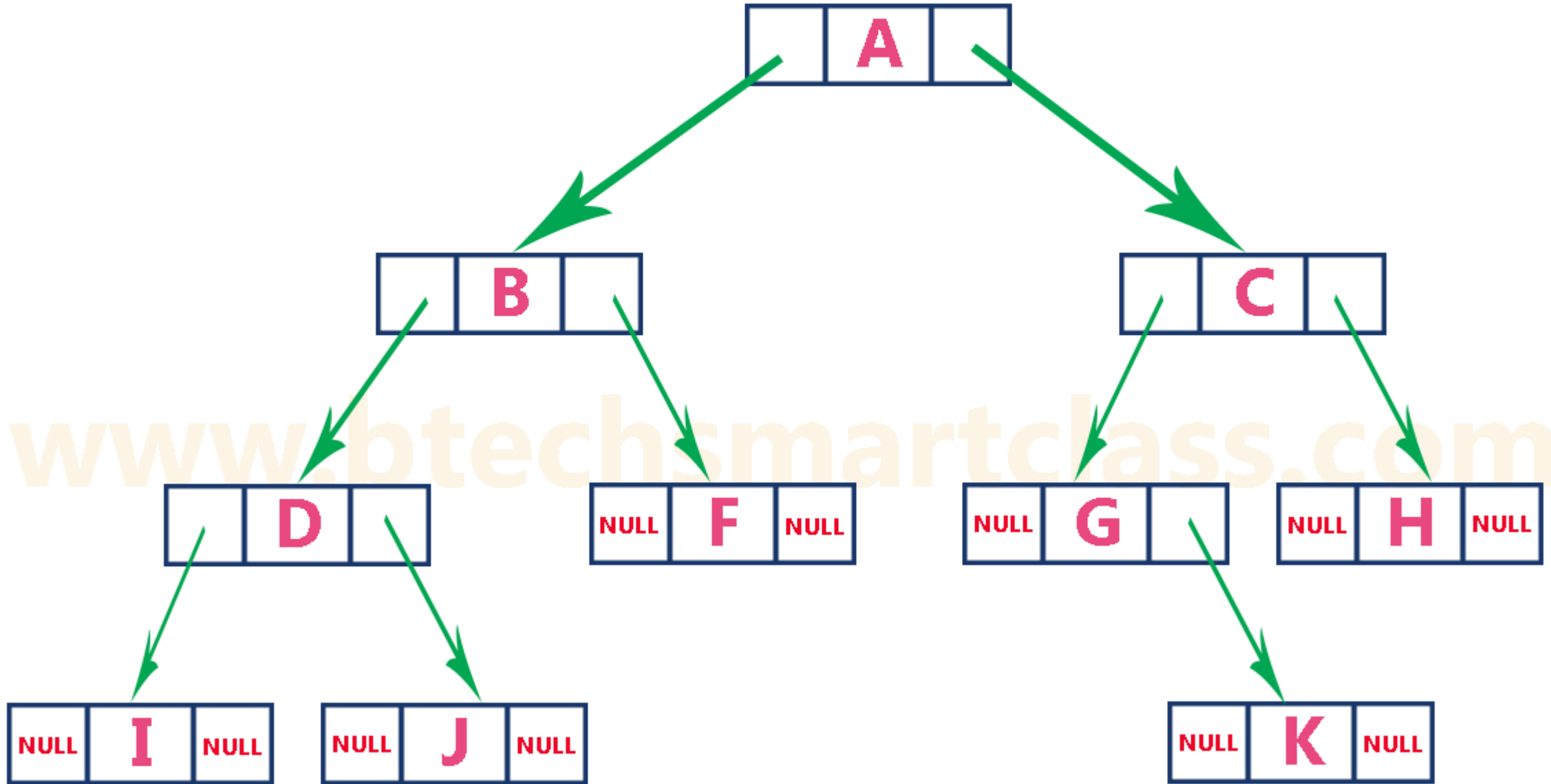
```
    public Node (String item) {  
        key = item;  
        left = right = null;  
    }
```



```
    public String toString () {  
        return key;  
    }  
}
```



rootNode



```
public class BinarySearchTree {  
    private Node root;
```

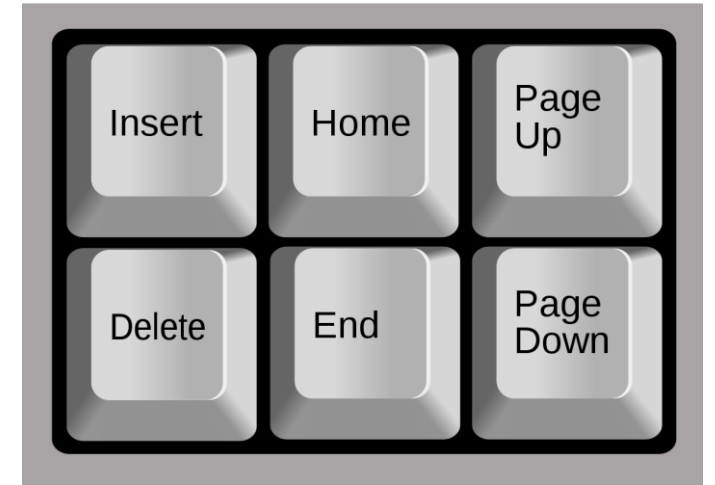
```
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        root = null;  
    }
```


Insert

If there is no node,
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```
BinarySearchTree t = new BinarySearchTree();  
t.insert(25);  
t.insert(15);  
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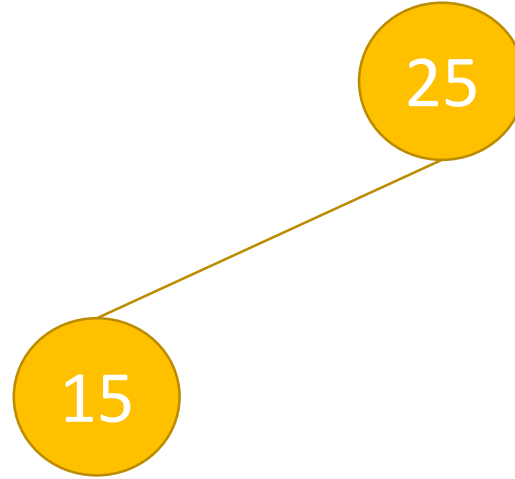


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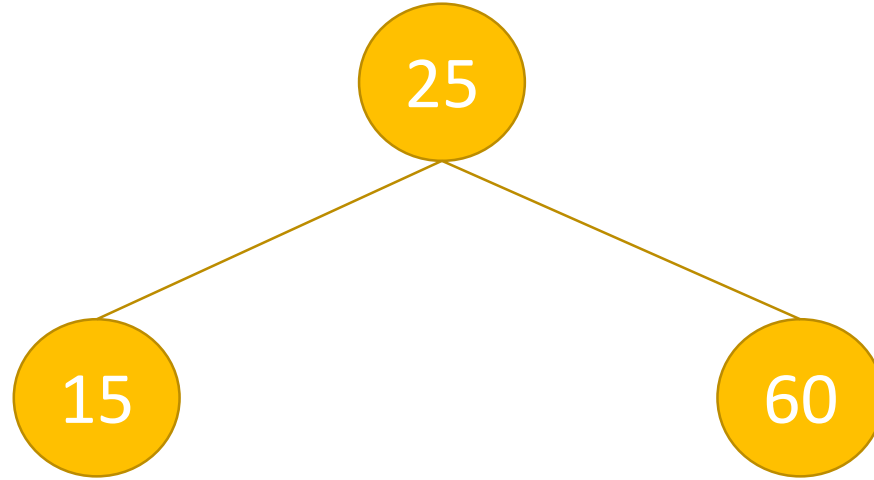


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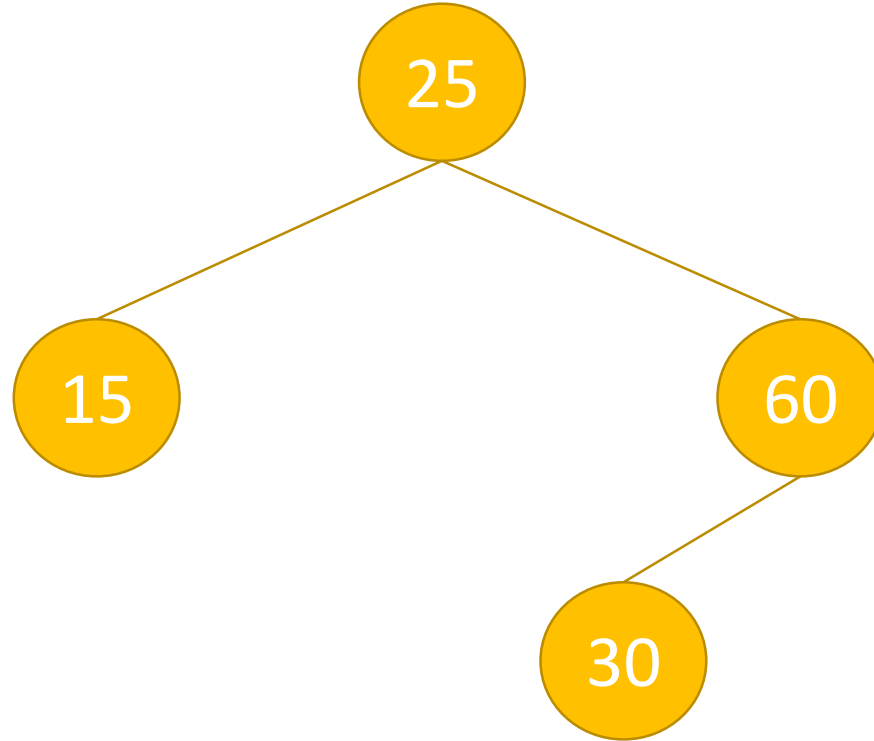


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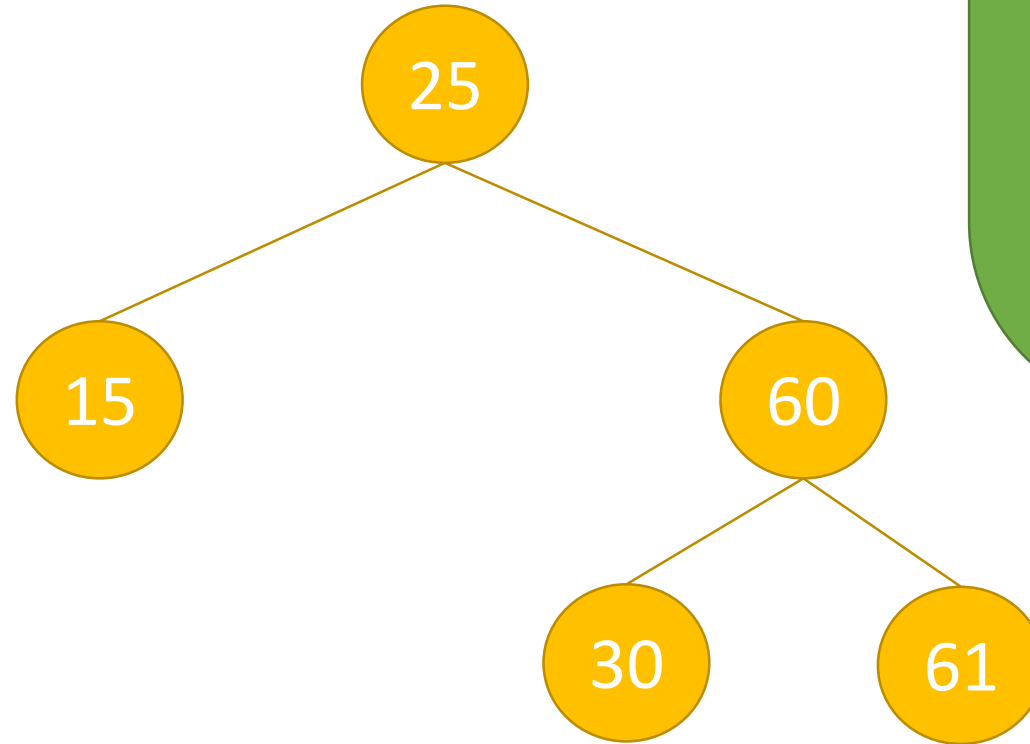


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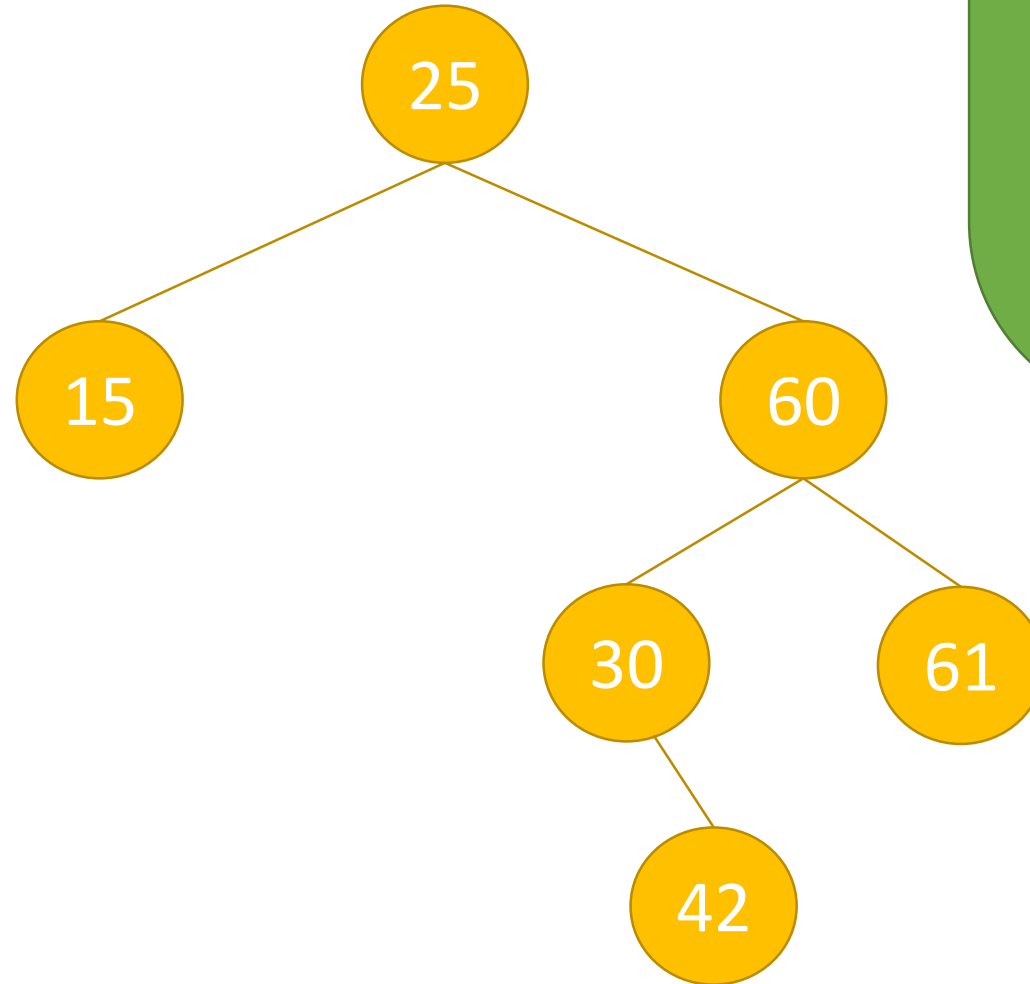


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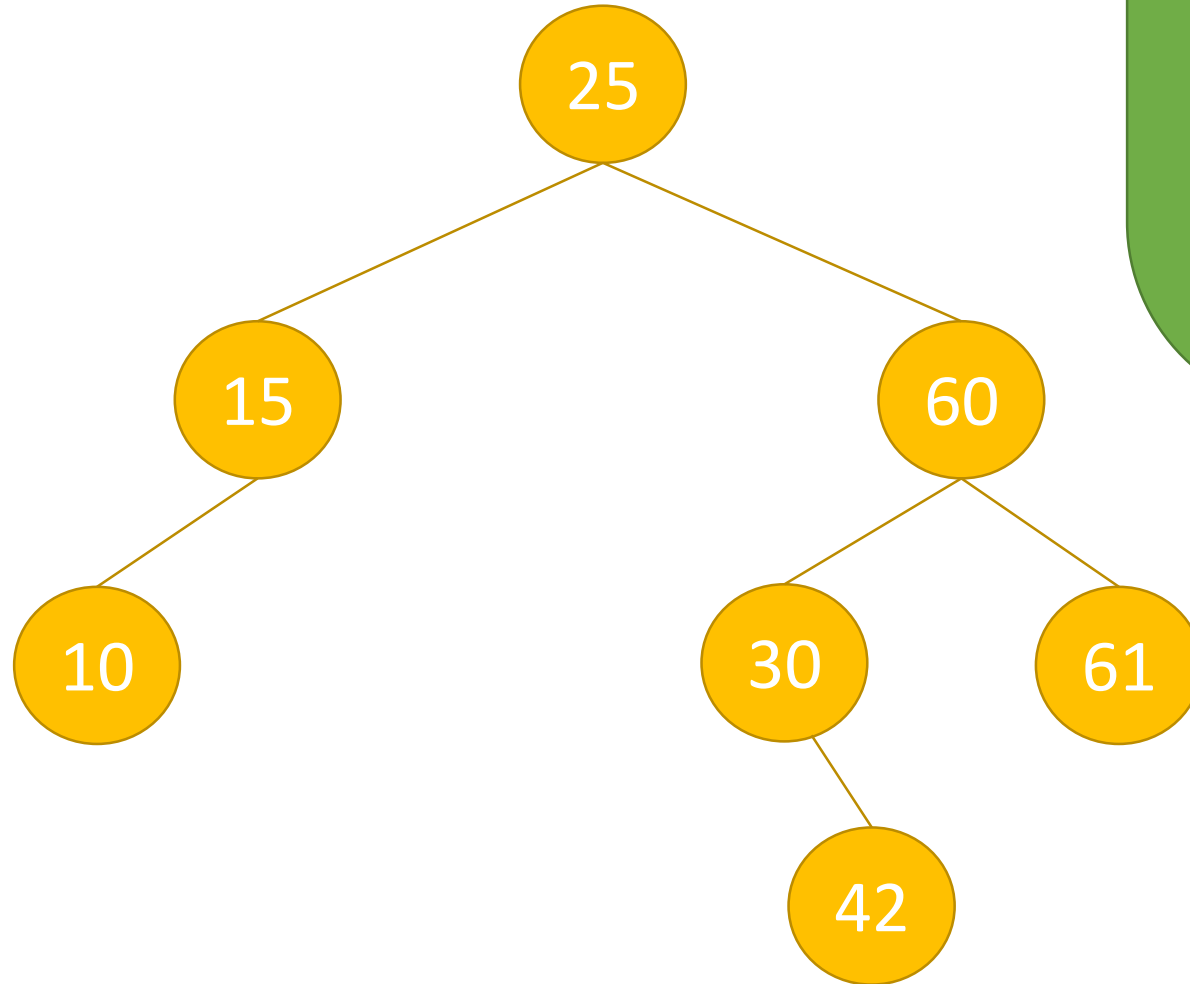


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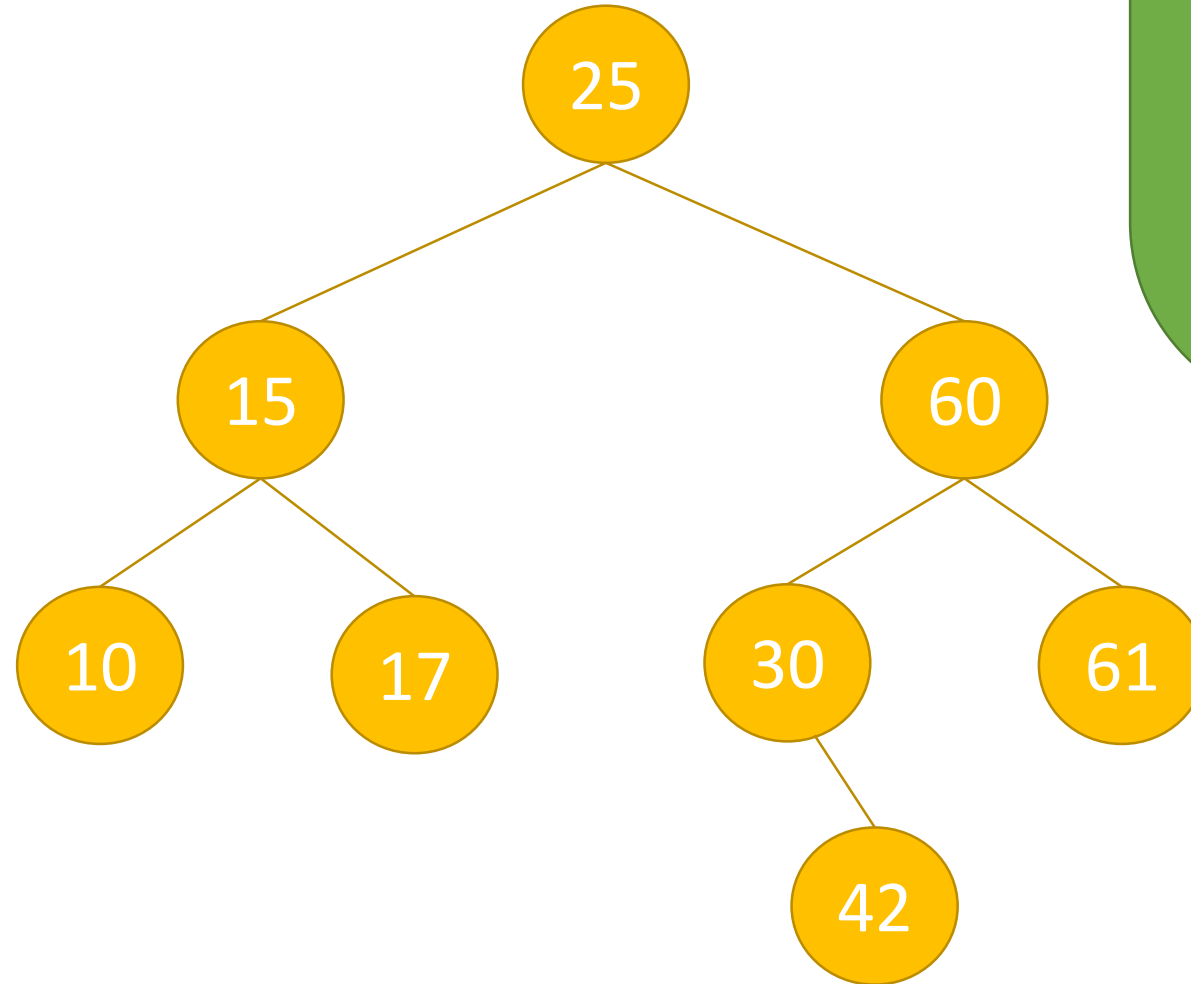


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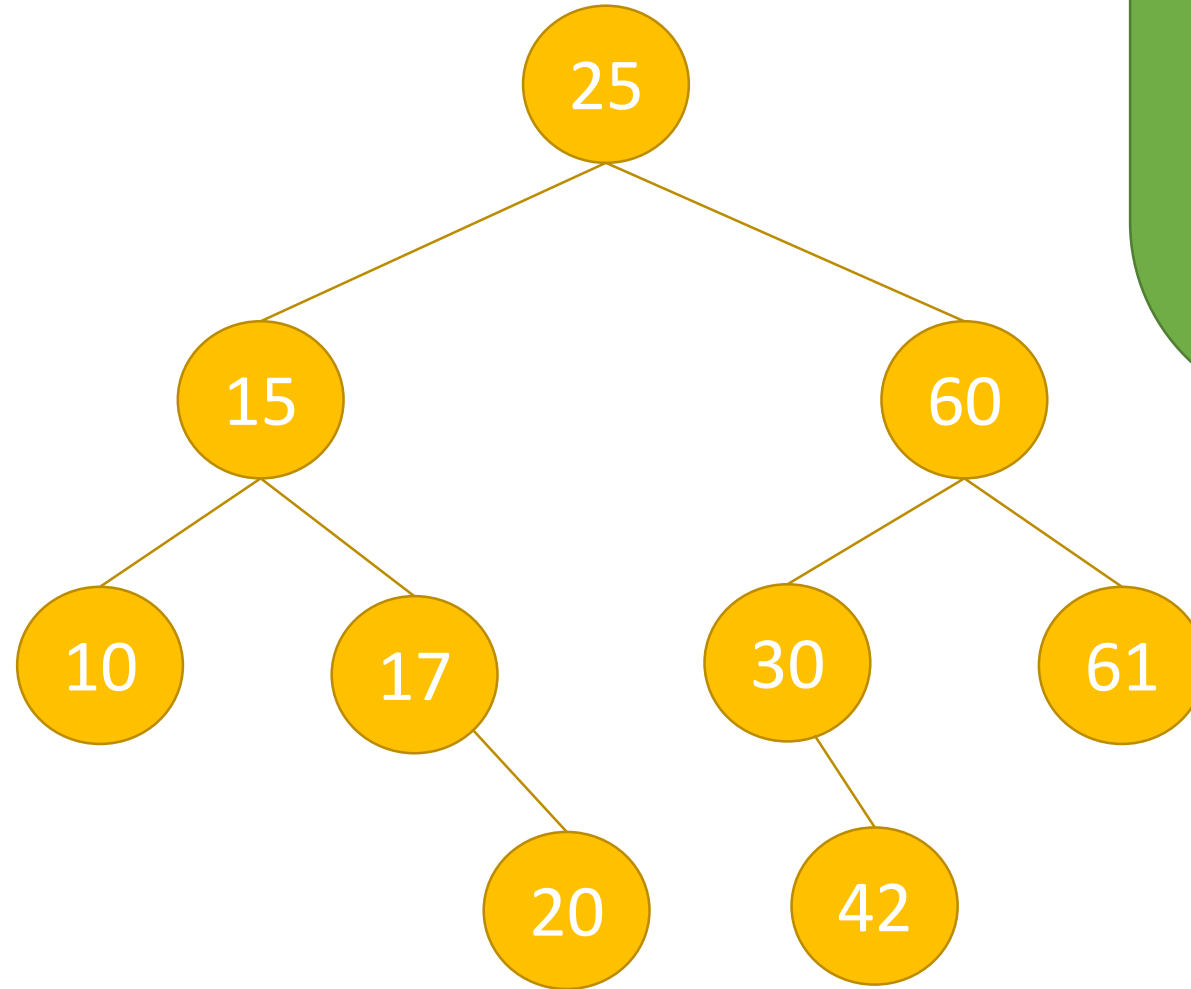


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t.insert("k");  
t.insert("c");  
t.insert("e");  
t.insert("f");  
t.insert("a");  
t.insert("w");  
t.insert("z");  
t.insert("p");
```

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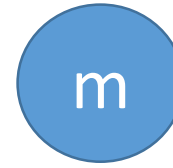
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t.insert("f");
```

```
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```

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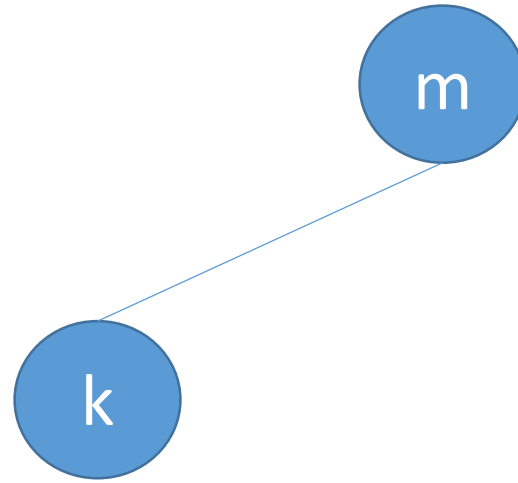
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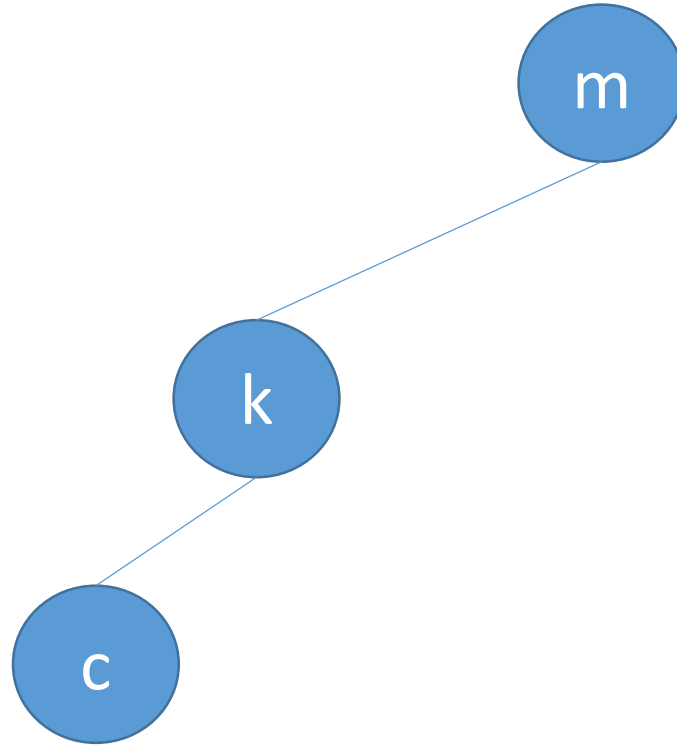
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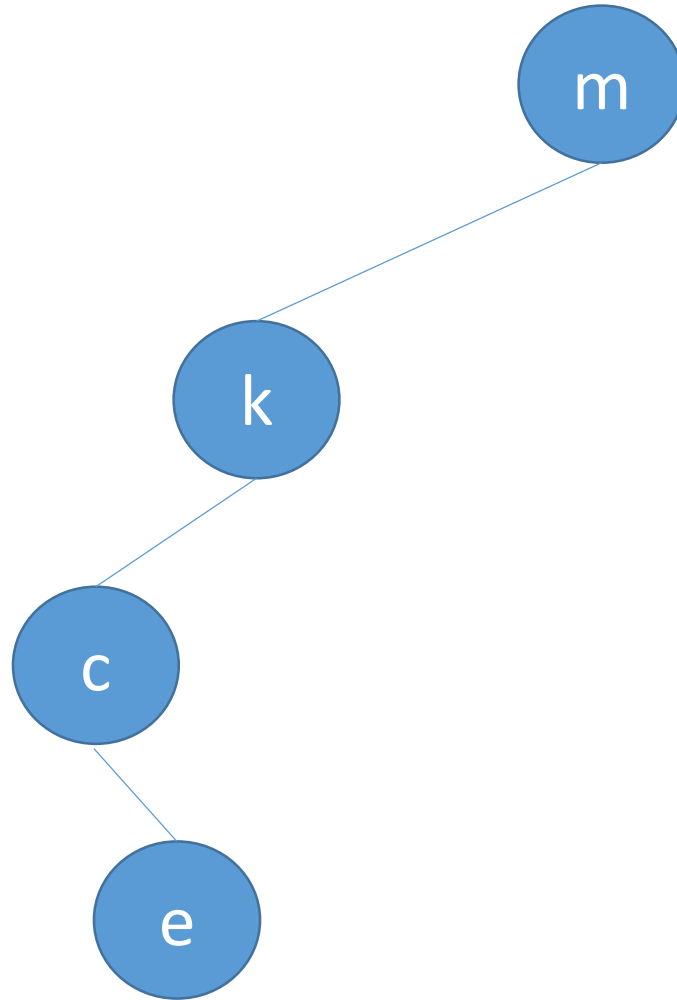
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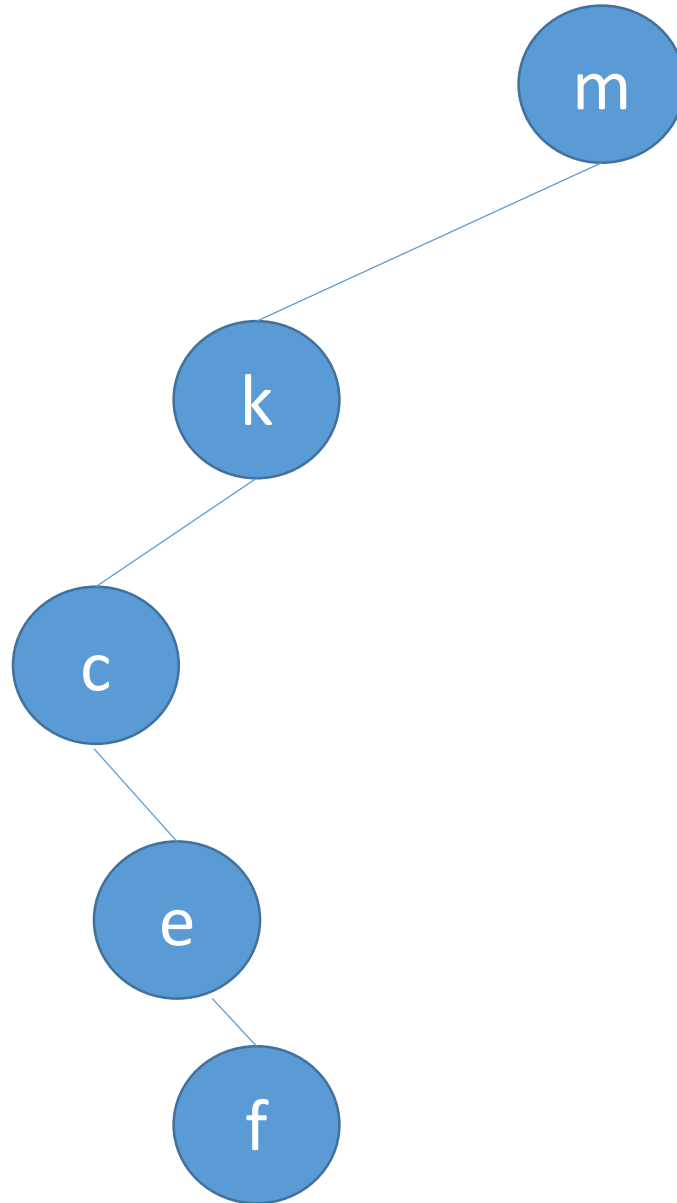
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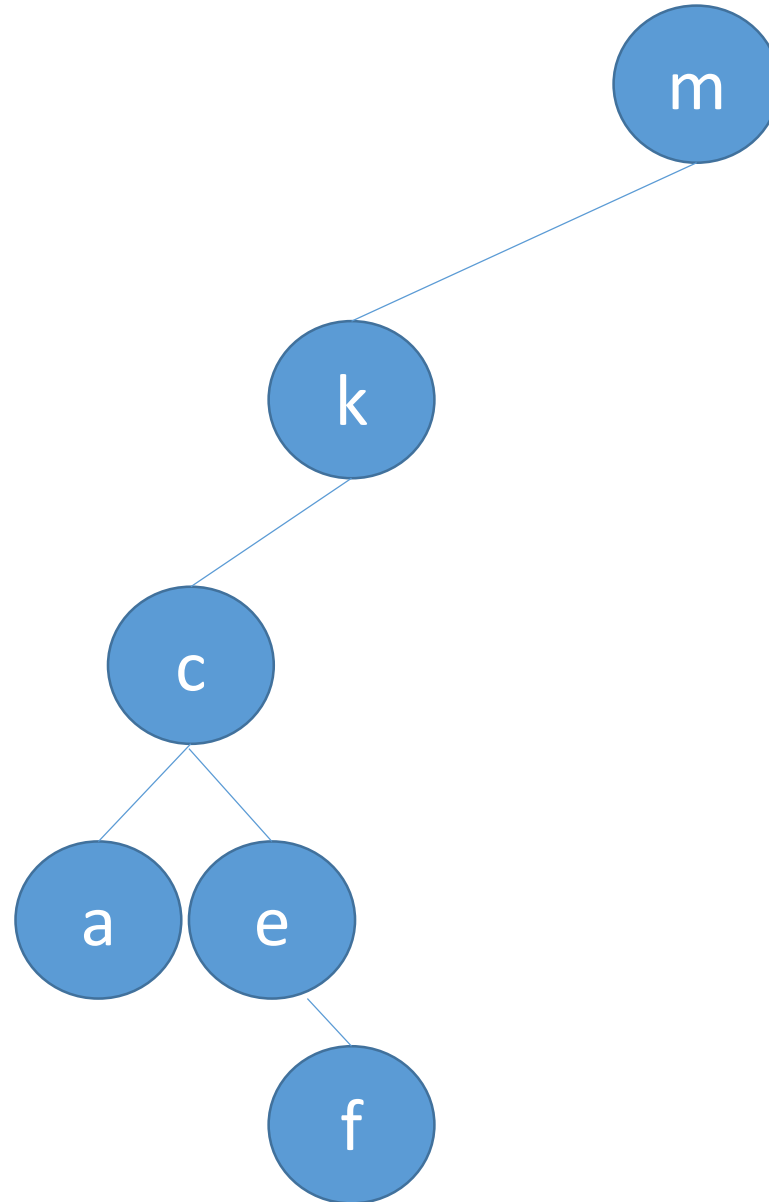
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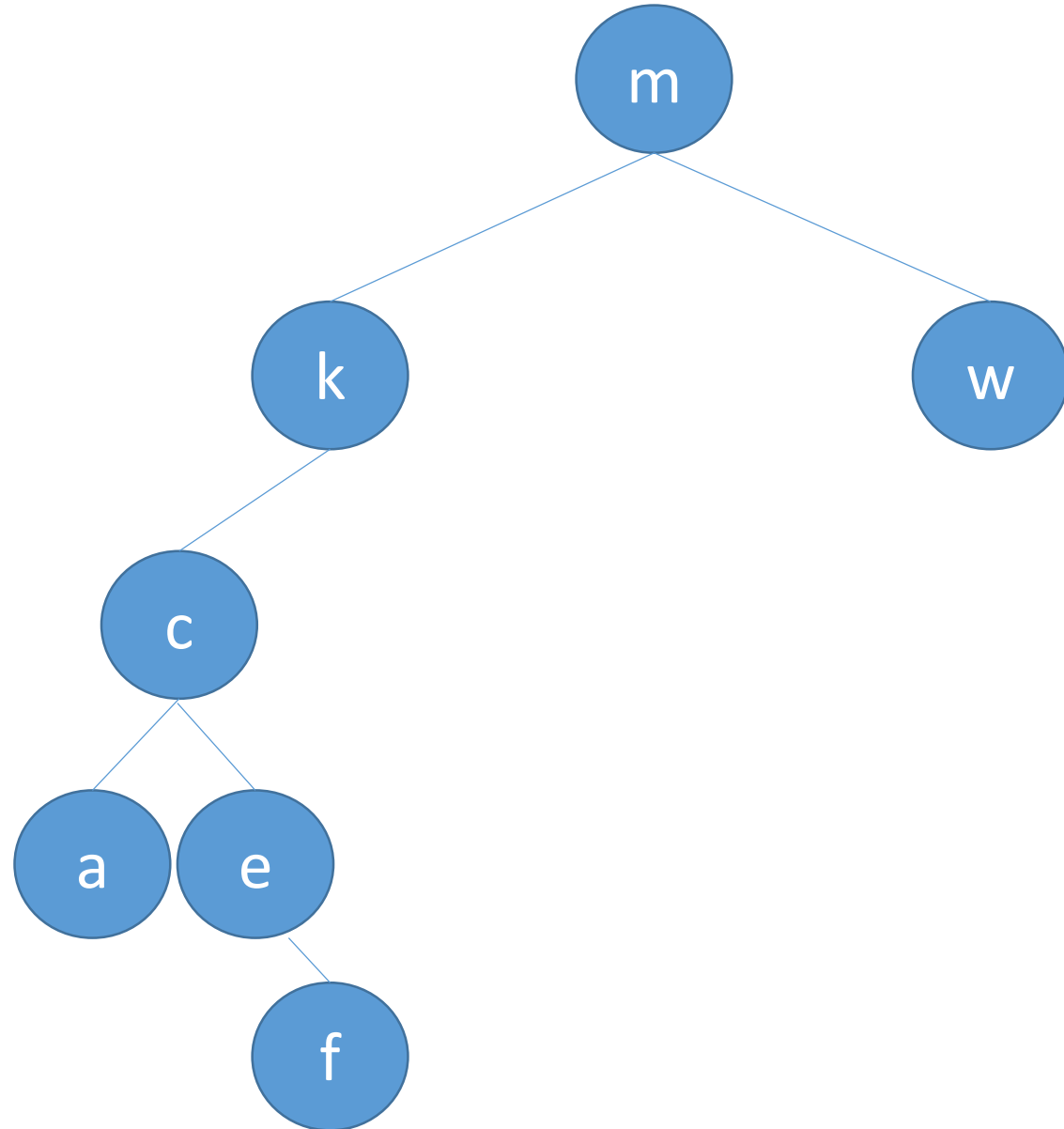
```
t.insert("p");
```

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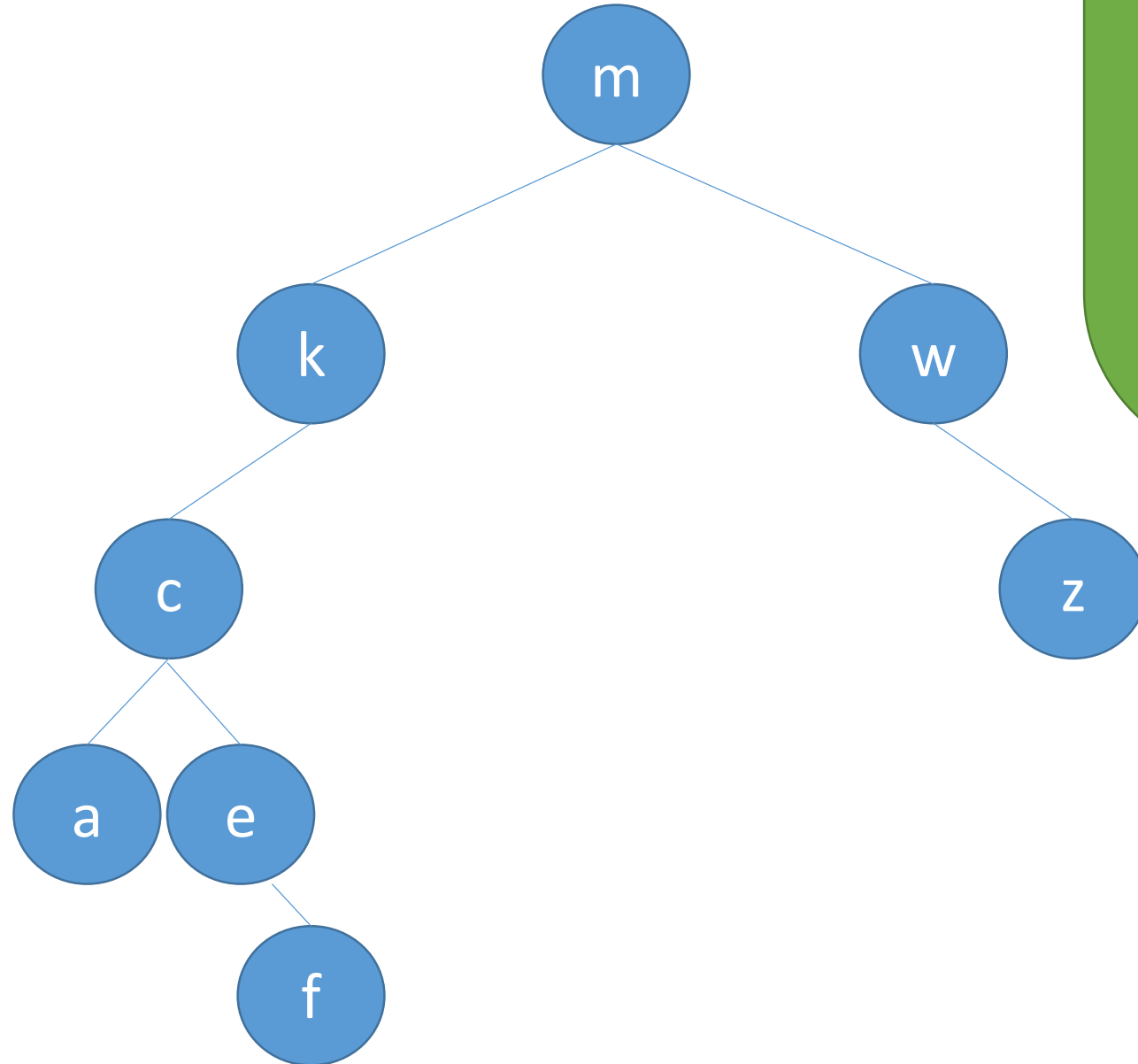
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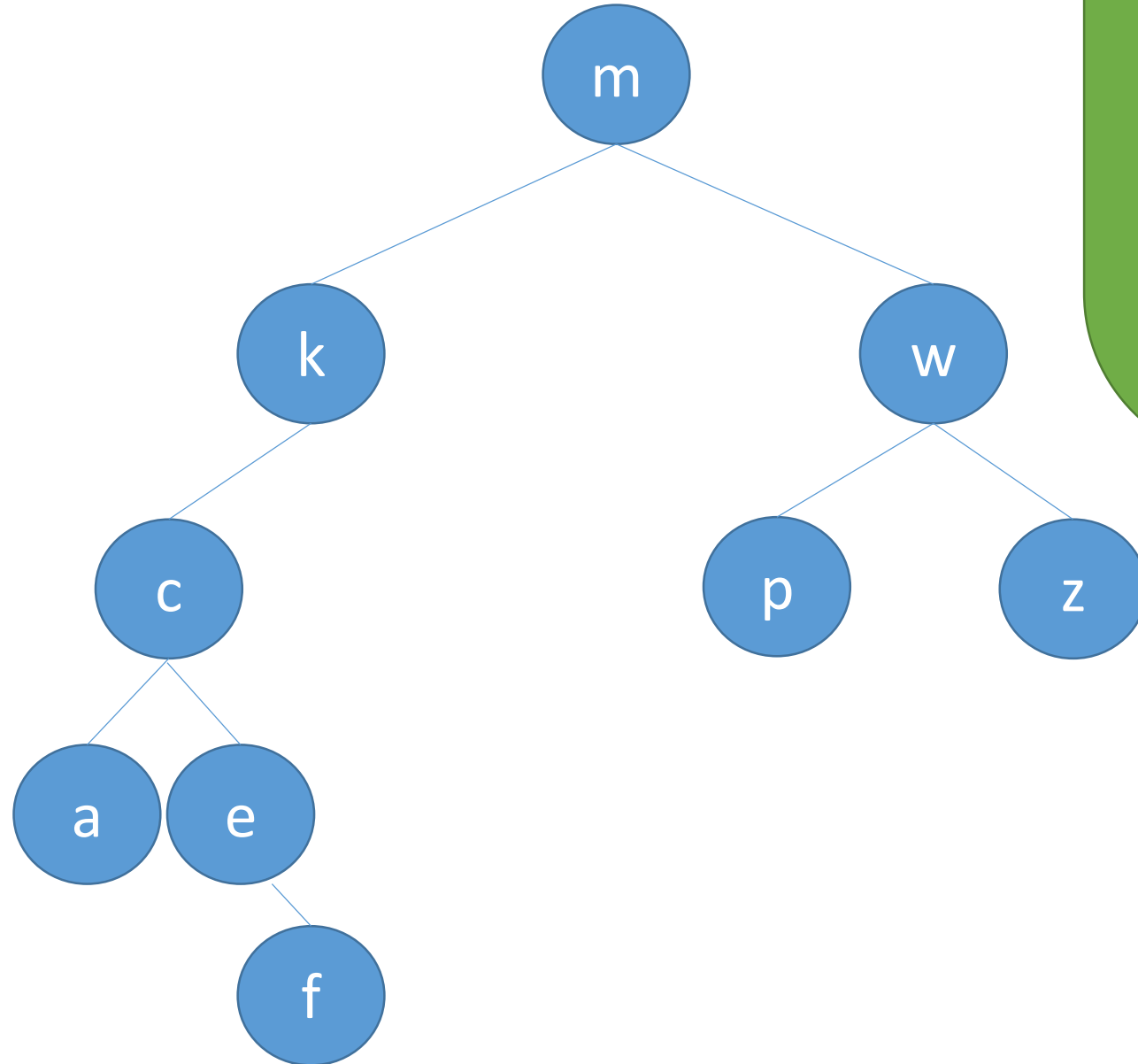
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```
private Node insertRec (Node root, String key) {  
    if (root == null) {  
        root = new Node (key);  
        return root;  
    }  
    else if (key.compareTo (root.key) < 0)  
        root.left = insertRec (root.left, key);  
    else if (key.compareTo (root.key) > 0)  
        root.right = insertRec (root.right, key);  
    return root;  
}
```

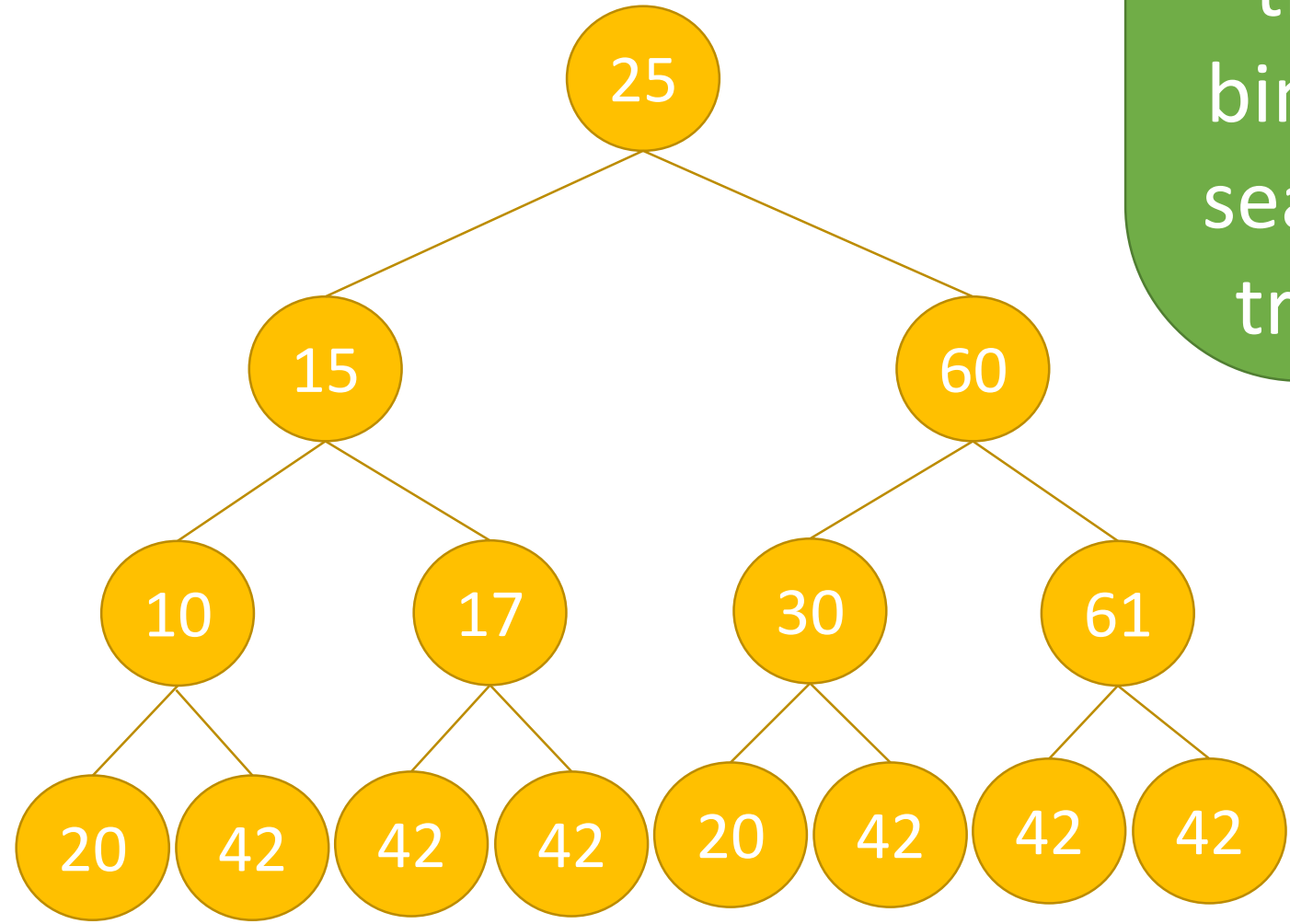
Why is a binary search tree useful?

- They are sorted and their order is useful
- They are very adaptable; easy to insert and delete
- They are FAST. Most functions: search, insert, delete, min, max are $O(\log n)$
- Used to “index” databases so searching is quick
- Used to store dictionaries
- IP address indexing
- Expressing arithmetic expressions

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